

# SUBSTITUENT EFFECTS IN SECOND ROW MOLECULES

## MOLECULAR ORBITAL STUDIES OF PHOSPHORUS(III) COMPOUNDS

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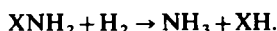
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(Received in UK 10 December 1984)

**Abstract**—Substituent effects in directly bonded P(III) compounds are investigated by *ab initio* MO calculations of relative energies and the results compared with those for the corresponding nitrogen species. The investigation covers substitution by X = BH<sub>2</sub>, CH<sub>3</sub>, NH<sub>2</sub>, OH, F in PHX<sup>−</sup>, PH<sub>2</sub>X, and PH<sub>3</sub>X<sup>+</sup> series molecules with some attention also to PX<sub>3</sub> and PX<sub>3</sub>H<sup>+</sup> species. Except for compounds containing the π-acceptor substituent BH<sub>2</sub>, σ-interactions dominate substitution behaviour but the second row species tolerate electron withdrawal better than their first row analogues, the severe destabilization of NH<sub>2</sub>X and NH<sub>3</sub>X<sup>+</sup> by σ-electron withdrawal being absent from PH<sub>2</sub>X and PH<sub>3</sub>X<sup>+</sup>. In contrast to the σ-withdrawing NH<sub>2</sub> group, the PH<sub>2</sub> group is characterized as a mild σ-donor. PH<sup>−</sup> is a σ-donor and PH<sub>3</sub><sup>+</sup> a σ-acceptor. π-Bonding to the second row atom is an important means of maintaining electroneutrality in the PH<sub>3</sub>X<sup>+</sup> series, where dπ functions have a bigger role than pπ functions.

Substituent effects in the first row hydrides CH<sub>4</sub>, NH<sub>3</sub>, H<sub>2</sub>O, and HF and related charged species NH<sub>4</sub><sup>+</sup>, NH<sub>3</sub><sup>+</sup>, OH<sup>−</sup> have been subjected to theoretical analysis by Radom *et al.* who made particular use of substituent interaction energy calculations.<sup>1</sup> The results were readily accommodated by simple perturbation molecular orbital theory and the known characteristics of the substituents used.

In relative energy calculations the effect of errors inherent in the Hartree-Fock approach is minimized by comparing systems with the same number of bonds. The case of the amines is typical:



In this case the substituent interaction energy measures the energy of the X—N interaction relative to the X—H interaction. Because of the exceptional strength of the X—H bonds, the interaction energy of this system is often negative and trends are more valuable than absolute values in rationalizing chemical behaviour.

Recently there have been several reports of high-level calculations of first row bases<sup>2</sup> which have concentrated on the calculation of accurate energies of protonation rather than an investigation of substituent effects but some conclusions about the nature of the bonding interactions and the effect of substituents were also drawn. Similar studies on some second row bases have also been published.<sup>3</sup>

Because of the importance of later main group molecules the relative energy approach is now extended to the second row by model calculations on some systems of phosphorus and, in other publications, on silicon and sulfur.<sup>4</sup> In this paper the series PH<sub>2</sub>X, PH<sub>3</sub>X<sup>+</sup>, and PHX<sup>−</sup> are treated (X = H, BH<sub>2</sub>, CH<sub>3</sub>, NH<sub>2</sub>, OH, F) and, for X = CH<sub>3</sub> and F only, the tri-substituted species PX<sub>3</sub> and PX<sub>3</sub>H<sup>+</sup>. Not all the systems modeled correspond to compounds yet isolated but the calculations were carried out on complete series for ease of comparison with earlier work.

### Method of calculation

The application of the Gaussian-80 series of programs<sup>5</sup> to compounds containing second row atoms at four basis set levels, with and without d-function supplementation, has been described separately.<sup>6</sup> The results selected for discussion in this paper are mainly from the calculations with the 6-31G<sup>++</sup> basis set.<sup>6b,7</sup> The geometries of all compounds were optimized at the 4-31G(♯) level by the gradient technique.

Calculations on the anionic series compounds PHX<sup>−</sup> were repeated with the use of diffuse s and p functions added to the 6-31G<sup>++</sup> basis, as recommended for first row anions by Spitznagel *et al.*<sup>7</sup> Preliminary calculations suggested the value *k* = 0.03 of the additional functions in the basis set, designated 6-31+G<sup>++</sup>. The corresponding first row NHX<sup>−</sup> series were also restudied in this way, using the recommended 4-31+G(♯) basis.<sup>7</sup>

### RESULTS

Energy data (at 6-31+G<sup>++</sup>, 6-31G<sup>++</sup> and 4-31G(♯) levels)<sup>6b</sup> and optimized geometries (4-31G(♯) level) for the PHX<sup>−</sup> series molecules are set out in Table 1 and Fig. 1, which also contain entries for PH<sub>2</sub>·BH<sub>2</sub> and PH<sub>3</sub>·BH<sub>2</sub><sup>+</sup>. Data for the remaining members of the PH<sub>2</sub>X and PH<sub>3</sub>X<sup>+</sup> series are reported elsewhere.<sup>6</sup> Energy data at the 4-31+G basis set level for the NHX<sup>−</sup> series compounds are also included in Table 1.

Substituent interaction energies (ΔE(X, H)) for the PHX<sup>−</sup>, PH<sub>2</sub>X and PH<sub>3</sub>X<sup>+</sup> series are presented in Table 2, results being listed for calculations at 4-31G(♯), 6-31G(♯), 6-31G<sup>++</sup>, and 6-31+G<sup>++</sup> basis set levels (for anions, at 6-31+G<sup>++</sup> and 4-31+G levels). The substituent interaction energies refer to the reactions:

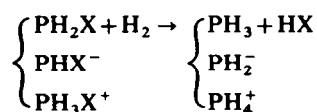


Table 1. Calculated total energies (Hartrees) of PHX<sup>-</sup> series molecules (X = H, BH<sub>2</sub>, CH<sub>3</sub>, NH<sub>2</sub>, OH, F), PH<sub>2</sub>·BH<sub>2</sub> and PH<sub>3</sub>·BH<sub>2</sub><sup>+</sup> and NHX<sup>-</sup> series molecules<sup>a</sup>

Basis set :	4-31G( # )	6-31G # #	6-31 + G # #
PH <sub>2</sub> <sup>-</sup> (C <sub>2v</sub> )	-341.42534	-341.84015	-341.85587
PH·BH <sub>2</sub> <sup>-</sup> (C <sub>s</sub> )	-366.69918	-367.13593	-367.14520
PH·CH <sub>3</sub> <sup>-</sup> (C <sub>s</sub> )	-380.40306	-380.86975	-380.88348
PH·NH <sub>2</sub> <sup>-</sup> (C <sub>s</sub> )	-396.37884	-396.86099	-396.88334
PH·OH <sup>-</sup>	-416.19603	-416.69675	-416.73400
PHF <sup>-</sup> (C <sub>s</sub> )	-440.20138	-440.70483	-440.73463
PH <sub>2</sub> ·BH <sub>2</sub> (C <sub>s</sub> )	-367.29286	-367.70779	
PH <sub>3</sub> ·BH <sub>2</sub> <sup>+</sup> (C <sub>s</sub> )	-367.61536	-368.03073	
Basis set :	4-31 + G		
NH <sub>2</sub> <sup>-</sup>	-55.44246		
NH·BH <sub>2</sub> <sup>-</sup>	-80.74276		
NH·CH <sub>3</sub> <sup>-</sup>	-94.40423		
NH·NH <sub>2</sub> <sup>-</sup>	-119.35527		
NH·OH <sup>-</sup>	-130.15972		
NH·F <sup>-</sup>	-154.16560		

<sup>a</sup> Energies at all levels calculated at the 4-31G( # ) optimized geometries.

Energies of protonation and deprotonation, both relative to those of the unsubstituted hydride PH<sub>3</sub>, are presented in Tables 2 and 3 which also include comparative material from published work on the corresponding first row compounds. The relative energies refer to the processes:

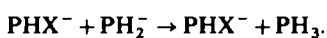
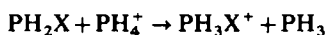


Figure 2 contains calculated interaction energies and  $\sigma$  and  $\pi$  bond orders for three second row series compounds with data for the corresponding nitrogen compounds. Taking the z-axis as the P—X internuclear axis,  $\sigma$  bond orders are Mulliken overlap populations for s and p<sub>z</sub> orbital overlap;  $\pi$  bond orders refer to total p<sub>x</sub> and p<sub>y</sub> orbital overlap.

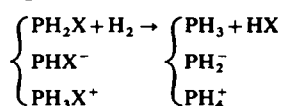
## DISCUSSION

The series of substituents considered in this research comprises the methyl group, capable of behaving as a donor or an acceptor, and the series of  $\sigma$ -acceptors NH<sub>2</sub>, OH, F which, by virtue of interactions with lone pairs of electrons, may also function as  $\pi$ -donors. Calculations were also carried out for substitution by the strong  $\pi$ -acceptor BH<sub>2</sub>.

A useful guide to the nature of the interactions expected for the five substituents is given by the substituent scales recently proposed by Topsom and co-workers.<sup>8</sup>  $\sigma_F(\text{theor.})$  is a field effect parameter, and  $\sigma_R(\text{theor.})$  an indication of the size of the resonance interaction of a substituent with a benzene ring.  $\sigma_X(\text{theor.})$  is a measure of group electronegativity on a scale in which the value for H is zero, so that negative

Table 2. Calculated substituent interaction energies for PHX<sup>-</sup>, PH<sub>2</sub>X, PH<sub>3</sub>X<sup>+</sup> series molecules (X = BH<sub>2</sub>, CH<sub>3</sub>, NH<sub>2</sub>, OH, F) with comparative data for NHX<sup>-</sup>, NH<sub>2</sub>X and NH<sub>3</sub>X<sup>+</sup> series (kJ mol<sup>-1</sup>)<sup>a,b,c</sup>

		X = BH <sub>2</sub>	CH <sub>3</sub>	NH <sub>2</sub>	OH	F
PHX <sup>-</sup>	6-31 + G # #	74.8	-110.7	-94.5	-61.9	-0.5
	6-31G # #	91.7	-105.5	-111.9	-89.5	-37.5
	4-31G( # )	133.8	-93.7	-70.4	-30.4	39.7
PH <sub>2</sub> X	6-31G # #	-15.7	-77.3	-67.0	-57.6	-26.4
	4-31G( # )	-16.6	-75.1	-36.4	-29.3	-4.3
PH <sub>3</sub> X <sup>+</sup>	6-31G # #	0.2	-12.9	3.7	-30.8	-43.8
	4-31G( # )	11.5	-4.0	35.7	6.0	-49.4
NHX <sup>-</sup>	4-31 + G	203.2	-135.5	-177.2	-170.7	-99.2
	4-31G	270.7	-92.6	-155.3	-144.8	-87.7
NH <sub>2</sub> X	4-31G	128.6	-127.1	-210.7	-254.9	-290.4
NH <sub>3</sub> X <sup>+</sup>	4-31G	-18.4	-82.7	-216.7	-324.1	-418.3

<sup>a</sup> Substituent interaction energies refer to the reactions:<sup>b</sup> All results from calculations on 4-31G( # )-optimized structures (4-31G-optimized structures for NHX<sup>-</sup> compounds).<sup>c</sup> Results from NH<sub>2</sub>X, NH<sub>3</sub>X<sup>+</sup> and NHX<sup>-</sup> 4-31G level calculations from refs. 1a,b.

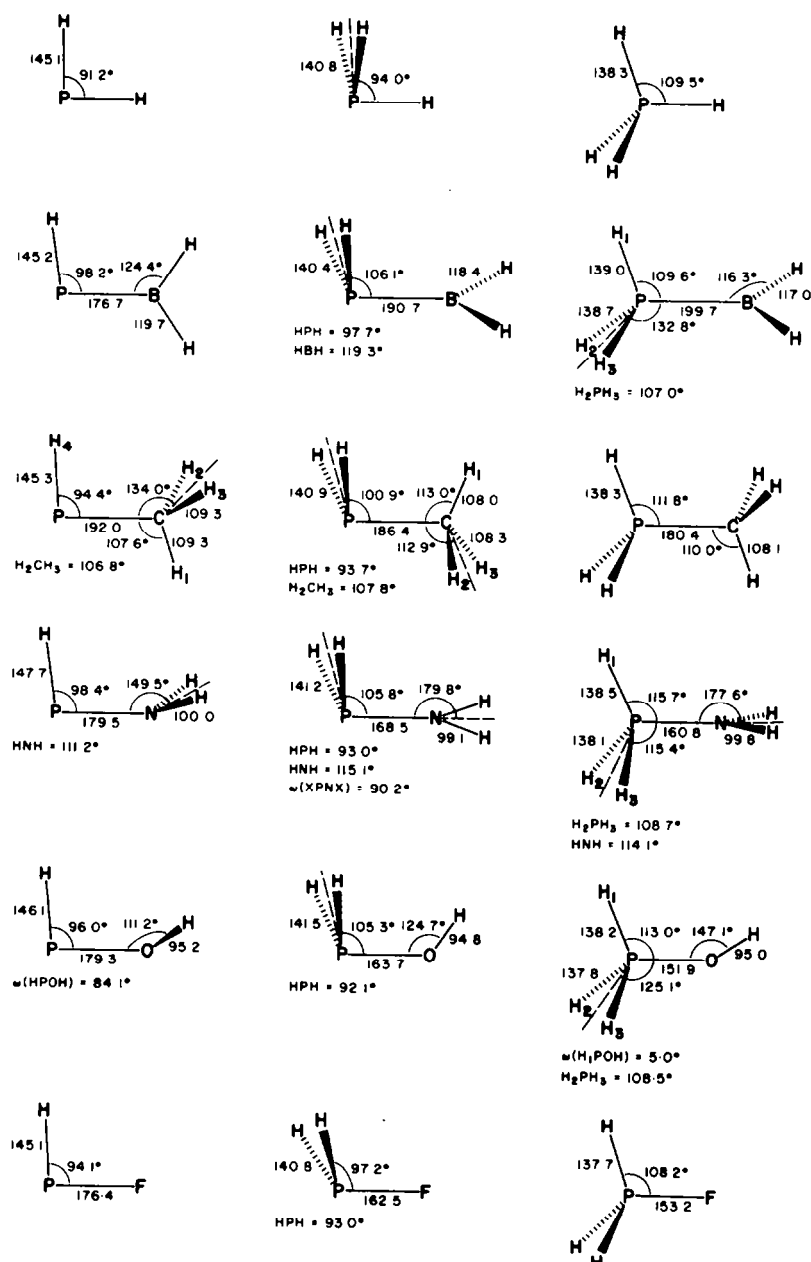


Fig. 1. Optimized geometries (4-31G( # ) level) for  $\text{PHX}^-$ ,  $\text{PH}_2\text{X}$  and  $\text{PH}_3\text{X}^+$  series molecules (bond lengths in pm, bond angles in degrees).

Table 3. Relative protonation and deprotonation energies of  $\text{PH}_2\text{X}$  series molecules ( $\text{X} = \text{BH}_2$ ,  $\text{CH}_3$ ,  $\text{NH}_2$ ,  $\text{OH}$ ,  $\text{F}$ ) with comparative data for  $\text{NH}_2\text{X}$  compounds\*

		$\text{X} = \text{BH}_2$	$\text{CH}_3$	$\text{NH}_2$	$\text{OH}$	$\text{F}$
Relative protonation energies						
$\text{PH}_2\text{X}$	6-31G # #	15.9	64.4	70.7	26.8	-17.5
	4-31G( # )	28.1	71.2	72.1	35.2	-45.1
$\text{NH}_2\text{X}$	4-31G	-110.3	44.4	-6.0	-69.2	-127.9
Relative deprotonation energies						
$\text{PH}_2\text{X}$	6-31 + G # #	91.4	-35.6	-58.0	-32.6	3.8
	6-31G # #	107.4	-28.2	-44.9	-31.9	-11.1
	4-31G( # )	150.4	-18.5	-34.0	-1.1	44.1
$\text{NH}_2\text{X}$	4-31 + G	74.6	-8.4	33.5	84.2	191.2
	4-31G	142.1	34.5	55.4	110.1	202.7

\*Details as for Table 2.

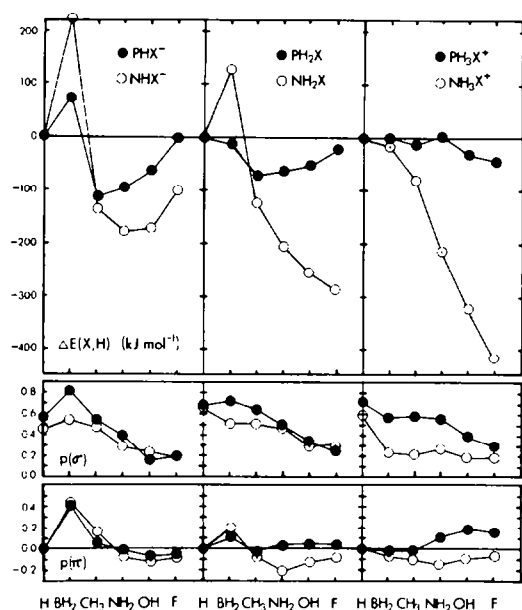


Fig. 2. Interaction energies ( $\text{kJ mol}^{-1}$ ) and calculated  $\sigma$  and  $\pi$  bond orders for  $\text{PH}_2\text{X}$  and  $\text{PH}_3\text{X}^+$  series molecules (6-31G $\#$ //4-31G $\#$ ) level calculations) and  $\text{PHX}^-$  series molecules (6-31 + G $\#$ //4-31G $\#$ ) level). Parallel results are included for  $\text{NHX}^-$ ,  $\text{NH}_2\text{X}$  and  $\text{NH}_3\text{X}^+$  series (4-31G//4-31G level calculations); energy data from refs. 1a,b.

values for less electronegative groups should be expected.

Group X:	$\text{BH}_2$	$\text{CH}_3$	$\text{NH}_2$	$\text{OH}$	$\text{F}$
$\sigma_X(\text{theor.})$	-0.09	0.17	0.33	0.43	0.52
$\sigma_F(\text{theor.})$	0.06	-0.02	0.16	0.31	0.49
$\sigma_R(\text{theor.})$	0.51	-0.03	-0.48	-0.44	-0.34

Comparison between first and second row systems is possible with the use of the values for the same parameters calculated by Topsom's procedures<sup>8</sup> for  $\text{PH}_2$ ,  $\text{PH}^-$ , and  $\text{PH}_3^+$ :

Second row center:	$\text{PH}_2$	$\text{PH}^-$	$\text{PH}_3^+$
$\sigma_X(\text{theor.})$	-0.05	-0.17	0.08
$\sigma_F(\text{theor.})$	0.09	-2.12	2.18
$\sigma_R(\text{theor.})$	-0.08	-0.80	0.09

These figures suggest that the  $\text{PH}_2$  group will act as a weak  $\sigma$ -acceptor, with weak  $\pi$ -donor ability in conditions that favour it. The responses to substitution by the  $\text{X} = \text{BH}_2$ ,  $\text{H}_3$ ,  $\text{NH}_2$ ,  $\text{OH}$ ,  $\text{F}$  series should be very much less pronounced than those shown by  $\text{NH}_2$ .<sup>1</sup> By extension, donor-acceptor interactions between substituents and the  $\text{PH}^-$  and  $\text{PH}_3^+$  groups are predicted to be weaker than in first row cases. However, Topsom's theoretical substituent scales take no account of the possible involvement of d functions, widely considered to play a small role in bonding to second row elements, even those of normal valency,<sup>9</sup> and it is of interest to observe the effect of their inclusion.

In situations where both  $\sigma$ - and  $\pi$ -type interactions can occur, it is necessary to determine which of the two is mainly responsible for the trends in the energy data or if both are contributing equally. Judicious use of electron population data may sometimes serve this purpose (see Fig. 2).

**Conformations and geometries of the substituted compounds.** In the few places where comparison is possible, the conformations and molecular dimensions obtained by geometry optimization at the 4-31G $\#$ ) level (Fig. 1) correspond closely to the experimentally determined values.<sup>10</sup> For  $\text{X} = \text{CH}_3$ ,  $\text{NH}_2$ ,  $\text{OH}$ ,  $\text{F}$  the  $\text{P-X}$  bond distances are longer in the anionic series than in the corresponding neutral compounds (average lengthening 10 pm) and shorter in the cationic series (average shortening 7 pm) which are similar to the figures for the corresponding  $\text{NHX}^-$ ,  $\text{NH}_2\text{X}$  and  $\text{NH}_3\text{X}^+$  series. As in substitution of nitrogen compounds by the  $\pi$ -acceptor  $\text{BH}_2$ , the  $\text{P-B}$  distances increase from  $\text{PH} \cdot \text{BH}_2^-$  to  $\text{PH}_2 \cdot \text{BH}_2$  to  $\text{PH}_3 \cdot \text{BH}_2^+$ , and by about the same amount, 20–25 pm.<sup>1a,7</sup> The  $\text{P-X}$  bonds are generally quite shorter than the sum of the covalent radii, particularly for the  $\text{OH}$  and  $\text{F}$  substituted compounds, in which the shortening is in the 10 to 20 pm range.

At the supplemented 4-31G basis set level,  $\text{XPH}$  and  $\text{HPH}$  bond angles are some  $10^\circ$  lower than  $\text{XNH}$  and  $\text{HNN}$  bond angles, simply because of steric constraints around the larger second row core.

The 4-31G $\#$ ) optimized conformations of the substituted phosphorus compounds are similar to those of the first row analogues<sup>1</sup> but the amino group is usually in a conformation which leaves the  $\text{PNH}_2$  fragment more closely planar than pyramidal. In the  $\text{OH}$ -substituted phosphorus compounds the  $\text{POH}$  bond angle is usually larger than it is in the corresponding first row compounds.

**Substituent effects.** The results obtained by Radom *et al.* for the sequence of changes induced in  $\text{NHX}^-$ ,  $\text{NH}_2\text{X}$  and  $\text{NH}_3\text{X}^+$  compounds by substitution with  $\text{CH}_3$ ,  $\text{NH}_2$ ,  $\text{OH}$  and  $\text{F}$  (Fig. 2) invite explanation in terms of  $\sigma$ -electron withdrawal from nitrogen;  $\pi$ -interaction with these substituents is too weak to mention.<sup>1</sup> Charge transfer away from nitrogen is expected to stabilize the anion and destabilize the cation, and this is observed, the neutral series being in an intermediate stabilizing position. However,  $\pi$ -interactions are much more important in the  $\text{BH}_2$ -substituted molecules as the results show dramatically in the comparison between the  $\text{NH}^-$  group (where  $\pi$ -bond formation is facilitated by the presence of a lone pair on the charged nitrogen species) and the  $\text{NH}_2$  and  $\text{NH}_3^+$  groups (where  $\pi$ -donation is much less likely).

The trends in the data for the P-containing species are most easily rationalized by ignoring  $\pi$ -electron interactions and classifying  $\text{PH}_2$  as a mild  $\sigma$ -electron donor,  $\text{PH}_3^+$  as a  $\sigma$ -acceptor and  $\text{PH}^-$  as a  $\sigma$ -donor. The exception is the strong  $\pi$ -interaction with  $\text{BH}_2$  in the anionic  $\text{PHX}^-$  series, but there is also a case for including  $\pi$ -interactions in explaining the data for the  $\text{PH}_2\text{X}$  and  $\text{PH}_3\text{X}^+$  series.

The greatest contrast between 1st and 2nd row results is found in the rising trend in the neutral  $\text{PH}_2\text{X}$  series molecules. On this data  $\text{NH}_2$  is a  $\sigma$ -electron acceptor and  $\text{PH}_2$  as  $\sigma$ -electron donor, which is not unreasonable in view of the positions of the groups in the electronegativity scale.

$\text{PH}_3^+$  may be classified as a  $\sigma$ -acceptor and a weak  $\pi$ -acceptor, the trend down the series  $\text{NH}_2$ ,  $\text{OH}$ , and  $\text{F}$  being due to the fact that destabilizing  $\sigma$ -electron withdrawal prevails over the expected favourable effect of  $\pi$ -electron gain.  $\pi$  Bond orders (Fig. 2) are moderate but the favourable effect is insufficient to reverse the

effect of  $\sigma$ -electron withdrawal by the  $\sigma$ -acceptor substituents. Calculated values of the  $p\sigma$  density on phosphorus show a big response to the  $\sigma$ -electron acceptors (a drop of 0.7 e over the  $X = \text{BH}_2 \cdots \text{F}$  sequence) but the equivalent rise in  $p\pi$  density is only 0.05 e.

The  $p\pi$ - $p\pi$  interactions in  $\text{PH}_3\text{X}^+$  compounds are necessarily hyperconjugative, a fact reflected in the weakening of the P—H bonds in the interaction with the  $\pi$ -acceptor  $\text{BH}_2$ , as attested both by bond orders and bond lengths. The  $p\pi$ - $p\pi$  part of the  $\pi$ -interactions between phosphorus and the  $\pi$ -donors  $\text{NH}_2$ ,  $\text{OH}$ ,  $\text{F}$  is too small to produce an identifiable effect; in any case, electrostatic (field) effects are the likely cause of any bond length changes with these substituents.

Analysis of the bond order results lends support to the above assignments,  $\pi$ -bonding having relatively little impact on the effect of  $\sigma$ -electron withdrawal by the substituents in the neutral and anionic series. Comparison of  $\Delta E(\text{X}, \text{H})$  trends across the substituent sequences with the calculated P—X bond orders shows an overall correspondence between the two. It is clear from the results for the charged nitrogen species that non-bonded interactions are important as well as the nature of the M—X bond; this is not repeated in the 2nd row molecules. However, in the  $\text{PH}_3\text{X}^+$  compounds, the effect of  $\pi$ -interactions is much more important, recalling the importance of  $\pi$ -bonding in the iso-structural, iso-electronic  $\text{SiH}_3\text{X}$  series.<sup>4a</sup> As in  $\text{SiH}_3\text{X}$  compounds, a large part of the  $\pi$  overlap density in the  $\text{PH}_3\text{X}^+$  series molecules is provided by d functions.<sup>9a</sup> Electron population data show that the d-type polarization functions reduce the progressive inductive withdrawal of charge from phosphorus by 0.1–0.2 e.

Polarization functions for second row atoms in supplemented basis sets are quite diffuse (exponents are obtained by optimization) but the size of the exponent increases from 0.45 to 0.55 to 0.65 from silicon to sulfur and the 0.55 value for phosphorus is sufficient to allow moderate  $d\pi$ - $p\pi$  overlap ( $2p\pi$ - $3d\pi$  overlap integrals are 0.16, 0.21 and 0.25 for Si—N, P—N and S—N bonds). The levels of utilization in the series considered here, especially in the  $\text{PH}_3\text{X}^+$  series, require them to be regarded as intermediate between polarization functions (functions added to improve flexibility in the wavefunction) and actual valence orbitals (high-lying, but accessible).

The  $d\pi$  contributions to P—X bonding are always favourable. Without these interactions, non-bonded repulsions would oblige the  $\pi$  bond orders in the  $\text{PH}_2\text{X}$  and  $\text{PHX}^-$  series compounds to be negative, as they are in the  $\text{NH}_2\text{X}$  and  $\text{NHX}^-$  series. Comparison calculations, performed with and without d function supplementation, show bond shortening in all the substituted compounds, but it is greatest (ca 10 pm) in the case where the d function contribution to bonding is the highest ( $\text{PH}_3\text{X}^+$ ).<sup>9a</sup>

The pattern of  $\pi$ -bonding interactions in the neutral and anionic series is as follows. Broadly, the  $p\pi$ - $p\pi$  interactions are anti-bonding in  $\text{PHX}^-$  and slightly anti-bonding in the neutral  $\text{PH}_2\text{X}$  compounds. The d function contribution increases as the charge on phosphorus moves to positive values. The net effect of the  $p\pi$ - and  $d\pi$ -interactions is bond weakening in the anions and very slightly bond strengthening in the neutral phosphines. The main reason for the rather small role for  $\pi$ -bonding in the  $\text{PH}_2\text{X}$  and  $\text{PHX}^-$  series

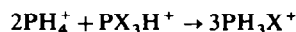
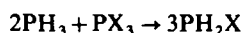
is conformational. Since the interactions between the lone pairs on  $\text{PH}_2$  and  $\text{X}$  are necessarily destabilizing, conformations are adopted in which they are minimized. Thus, the lone pair directions are perpendicular in the minimum energy conformations (gauche) of  $\text{PH}_2 \cdot \text{NH}_2$  and  $\text{PH}_2 \cdot \text{OH}$ . For these compounds there is a 35 kJ mol<sup>-1</sup> energy advantage gained by rotation about the P—X bond from the eclipsed conformation.

The characterization of  $\text{PH}_3^+$  as a weak  $\sigma$ -acceptor and a weak  $\pi$ -acceptor is consistent with ESR and electrochemical results for P and N ring compounds, explained in terms of P-ring hyperconjugation.<sup>11</sup> Also relevant to the calculated properties of the  $\text{PH}_2$  and  $\text{PH}_3^+$  groups are <sup>13</sup>C-NMR measurements on  $\text{PR}_2$ -substituted benzene made by Modro, who obtained values of the inductive and resonance parameters for  $\text{PMe}_2$  of  $\sigma_I = 0.06$  and  $\sigma_R = -0.02$ .<sup>12</sup> The values for the  $\text{PH}_2$  group should be quite close to these. For phosphonium compounds, however, NMR measurements point to the existence of a strong resonance component.<sup>13</sup>

*Tri-substituted compounds.* Data for the tri-substituted  $\text{PX}_3$  and  $\text{PX}_3\text{H}^+$  compounds (methyl and fluorine substituents only) are given in Table 4; calculations were performed at the 4-31G(♯) level.

The results on the fully substituted molecules provide information about the effect on phosphorus donor-acceptor properties of progressive addition of substituents, it being obvious that the  $\Delta E(\text{X}, \text{H})$  values for tri-substitution are far from three times the values for mono-substitution. This implies non-additivity, resulting from interaction between different P—CH<sub>3</sub> and P—F bonds.

The departure of  $\Delta E(\text{X}, \text{H})$  values from linearity in the degree of substitution is equal to the relative energy of the bond separation process:



For  $\text{X} = \text{F}$ , these are large and positive, which is interpreted to mean that P—F interaction becomes progressively more stabilizing as fluorine atoms are added, in contrast to the opposite effect of added methyl groups. For the bond separation processes above, the substituent interaction energies are:

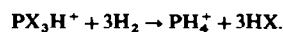
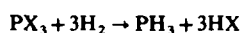
$\Delta E(\text{X}, \text{H}); \text{kJ mol}^{-1}$	$\text{X} = \text{CH}_3$	$\text{X} = \text{F}$
$\text{PH}_2\text{X}$	-28.0	153.1
$\text{PH}_3\text{X}^+$	-51.2	103.3

These responses are to be expected if  $\text{PH}_2$  is a mild  $\sigma$ -

Table 4. Calculated substituent interaction energies of  $\text{PX}_3$ ,  $\text{PX}_3\text{H}^+$  series molecules ( $\text{X} = \text{CH}_3, \text{F}$ )<sup>a, b</sup>

$\text{P}(\text{CH}_3)_3$	-253.6
$\text{PF}_3$	148.5
$\text{P}(\text{CH}_3)_3\text{H}^+$	-63.2
$\text{PF}_3\text{H}^+$	-45.2

<sup>a</sup> Interaction energies refer to the processes:



<sup>b</sup> 4-31G(♯)//4-31G(♯) level calculations.

donor interacting with a  $\sigma$ -electron donor ( $X = \text{CH}_3$ ) and a  $\sigma$ -electron acceptor ( $X = \text{F}$ ).

In the  $\text{PX}_3\text{H}^+$  compounds the effects of donation by  $\text{CH}_3$  and withdrawal by F are partly quenched by the weak  $\sigma$ -acceptor character of the second row group. The results suggest that  $\sigma$ -withdrawal and  $\pi$ -donation are in competition, also attested by the very large d function occupation in  $\text{PF}_3\text{H}^+$  ( $q(3d) = 0.58$ ) chiefly in  $d\pi$  orbitals.

**Protonation and deprotonation.** Although the relative energy results listed in Table 3 were obtained to allow study of substituent effect trends, comparison with experiment is possible for the methyl compounds (Taft's compilation<sup>16</sup>). The protonation  $\Delta H$  values, relative to the protonation of  $\text{PH}_3$ , are  $64.4 \text{ kJ mol}^{-1}$  ( $\text{PH}_2\text{CH}_3$ ) and  $161.5 \text{ kJ mol}^{-1}$  ( $\text{P}(\text{CH}_3)_3$ ).<sup>16</sup> The calculated values are  $64.4 \text{ kJ mol}^{-1}$  and  $190.4 \text{ kJ mol}^{-1}$ , respectively.

These processes conform to the "isodesmic" criterion<sup>15</sup> and interaction energies are therefore expected to be less sensitive to basis set variation than those mentioned above. The relative protonation energy values for the substituted phosphines  $\text{PH}_2\text{X}$  (the difference between  $\Delta E(X, \text{H})$  for the  $\text{PH}_3\text{X}^+$  and  $\text{PH}_2\text{X}$  species) are seen to drop very rapidly across the series, the destabilization of  $\text{PH}_3\text{X}^+$  being reinforced by the stabilization of  $\text{PH}_2\text{X}$ . Although the nitrogen interaction energies change much more rapidly in response to  $\text{NH}_2$ , OH and F substitution, the effects on  $\text{NH}_2\text{X}$  and  $\text{NH}_3\text{X}^+$  are opposed and the trend across the series is close to that for  $\text{PH}_2\text{X}$  basicity.

The reverse situation is found for  $\text{PH}_2\text{X}$  and  $\text{NH}_2\text{X}$  deprotonation energies, the extreme sensitivity of the  $\text{NH}_2\text{X}$  proton abstraction process to substitution being the result of progressive destabilization of the neutral acid added to stabilization of the anion through the series. The two effects are opposed in the phosphorus series and the overall response to substitution is small.

## CONCLUSIONS

Relative energy calculations show that  $\sigma$ -interactions usually dominate substituent effects in directly bonded phosphines ( $\text{PH}_2\text{X}$ ) and in the related anionic ( $\text{PHX}^-$ ) and cationic ( $\text{PH}_3\text{X}^+$ ). Compared with the corresponding nitrogen species, responses of the second row compounds to  $\sigma$ -donor/ $\sigma$ -acceptor interactions are smaller, as are also  $\pi$ -interactions. Except for  $X = \text{BH}_2$ , where  $\pi$ -donation dominates the differences between  $\text{PHX}^-$ ,  $\text{PH}_2\text{X}$ , and  $\text{PH}_3\text{X}^+$ , the 2nd row series show only a shadow of the progressively stronger destabilization produced by  $\sigma$ -withdrawal from  $\text{NH}^-$ ,  $\text{NH}_2$ , and  $\text{NH}_3^+$ .

The groups may be characterized as follows:

- (a)  $\text{PH}_2$  is a weak  $\sigma$ -donor.
- (b)  $\text{PH}^-$  is a  $\sigma$ -donor and a  $\pi$ -donor.
- (c)  $\text{PH}_3^+$  is a weak  $\sigma$ -acceptor and a weak  $\pi$ -acceptor,

the latter function being due to a marginal bonding role for d functions.

## REFERENCES

- <sup>1a</sup>  $\text{NH}_2\text{X}$ ,  $\text{OHX}$ ,  $\text{FX}$ ,  $\text{OX}^-$ ,  $\text{NHX}^-$ : A. L. Hinde, A. Pross and L. Radom, *J. Computational Chem.* **1**, 118 (1980); <sup>b</sup>  $\text{NH}_3\text{X}^+$ ,  $\text{CH}_3\text{X}$ ,  $\text{BH}_3\text{X}^-$ : A. Pross and L. Radom, *Tetrahedron* **36**, 673 (1980); <sup>c</sup>  $\text{CH}_2\text{X}^-$ : A. Pross, D. J. DeFrees, B. A. Levi, S. K. Pollack, L. Radom and W. J. Hehre, *J. Org. Chem.* **46**, 1693 (1981).
- <sup>2</sup> J. E. Del Bene, M. J. Frisch, K. Raghavachari and J. A. Pople, *J. Phys. Chem.* **86**, 1529 (1982); A. Scheiner, *Chem. Phys. Lett.* **93**, 540 (1982); R. A. Eades, D. A. Weil, D. A. Dixon and C. H. Douglass, Jr., *J. Phys. Chem.* **85**, 981 (1981).
- <sup>3</sup> C. Glidewell and C. Thomson, *J. Computational Chem.* **3**, 495 (1982); D. S. Marynick, K. Scanlon, R. A. Eades and D. A. Dixon, *J. Phys. Chem.* **85**, 3364 (1981).
- <sup>4a</sup> Substituted silicon compounds  $\text{SiH}_3\text{X}$ ,  $\text{SiH}_2\text{X}^-$ , *Tetrahedron* (1985), in press; <sup>b</sup> substituted sulfur compounds  $\text{SHX}$ ,  $\text{SX}^-$ ,  $\text{SH}_2\text{X}^+$ , *Tetrahedron* (1985), in press.
- <sup>5</sup> J. S. Binkley, R. A. Whiteside, R. Krishnan, R. Seeger, D. J. DeFrees, H. B. Schlegel, S. Topiol, L. R. Kahn and J. A. Pople, *Quantum Chemistry Program Exchange* **12**, 406 (1980).
- <sup>6a</sup> E. A. Magnusson, *J. Computational Chem.* **5**, 612 (1984); <sup>b</sup> The basis sets designated 4-31G(♯) and 6-31G♯♯ in this work contain five d-functions rather than the six recommended by M. S. Gordon, J. S. Binkley, J. A. Pople, W. J. Pietro and W. J. Hehre, *J. Am. Chem. Soc.* **104**, 2797 (1982). The use of five d functions facilitates comparison of results obtained with and without supplementation. The results differ in energy but not in any other significant way.
- <sup>7</sup> G. W. Spitznagel, T. Clark, J. Chandrasekhar and P. v. R. Schleyer, *J. Computational Chem.* **3**, 363 (1982); J. Chandrasekhar, J. G. Andrade and P. v. R. Schleyer, *J. Am. Chem. Soc.* **103**, 5609 (1981).
- <sup>8</sup> R. D. Topsom, *Accts. Chem. Res.* **16**, 292 (1983), and references therein; *J. Am. Chem. Soc.* **106**, 7 (1984).
- <sup>9a</sup> E. A. Magnusson, *Accts. Chem. Res.* (1985), in press; <sup>b</sup> D. A. Dixon, T. H. Dunning, Jr., R. A. Eades and P. G. Gassman, *J. Am. Chem. Soc.* **105**, 7011 (1983).
- <sup>10</sup> W. J. Pietro, M. M. Francl, W. J. Hehre, D. J. DeFrees, J. A. Pople and J. S. Binkley, *J. Am. Chem. Soc.* **104**, 5039 (1982).
- <sup>11</sup> W. Kaim, U. Lechner-Knoblauch, P. Hanel and H. Bock, *J. Org. Chem.* **48**, 4206 (1983); C. K. White and R. D. Rieke, *Ibid.* **43**, 4638 (1978).
- <sup>12</sup> T. A. Modro, *Can. J. Chem.* **55**, 3681 (1977).
- <sup>13</sup> G. P. Schiemenz, *Angew. Chem. Int. Ed. Engl.* **7**, 545 (1968).
- <sup>14</sup> As reported elsewhere,<sup>6a,9a</sup> the addition of d functions to minimal basis sets exaggerates their importance to the energies and the wave functions of second row molecules. However, both the energy increment and the level of utilization of d functions are stable for supplemented 3-21G, 4-31G and 6-31G basis sets, suggesting that the "superposition effect" is small in basis sets of split-valence quality or better.
- <sup>15</sup> W. J. Hehre, R. Ditchfield, L. Radom and J. A. Pople, *J. Am. Chem. Soc.* **92**, 4796 (1970).
- <sup>16</sup> R. W. Taft, personal communication. Similar values from a variety of sources are cited by A. Ikuta, P. Kebarle, G. M. Bancroft, T. Chan and R. J. Puddephatt, *J. Am. Chem. Soc.* **104**, 5899 (1982).